CLAIMS

We Claim:

1. A method for optimizing a multivariate representation of resources which are used in producing a set of products, the resources, products and their respective connectivities being represented in a product space plan, the method comprising:

converting an expected value function associated with the resources and products into a closed form expression;

transforming the product space plan into a working transformed space plan, wherein the products are transformed into working elements;

performing a loading step to form elemental blocks as a function of a single variable with elements being loaded with resources that gate production of the element;

performing a re-loading step to form elemental blocks as a function of a single variable with elements being reloaded with resources that gate production of the element;

solving for the maximum of each elemental block over each associated single variable; and

determining the optimum level of resources as a function of the solved for maximums.

- 2. The method of Claim 1, wherein the loading and re-loading steps result in an equilibrium configuration that provides the minimum amount of resources to produce any given amount of products across the whole plan.
 - 3. The method of Claim 1, wherein the loading step further includes: sequentially looking at each present working element;

determining if each associated resource gates production of the element,

if gating occurs, then unloading the resource from a prior element if so loaded, and

loading the resource onto the present element.

4. The method of Claim 3, wherein the reloading step further includes: sequentially looking at each present working element; reloading each unloaded resource back onto the element; redetermining if the element is gated by each reloaded resource;

if the element is so gated, then merging the elements sharing each gating resource into a common elemental block which is a function of a single variable.

- 5. The method of Claim 3, wherein step of determining that gating occurs includes calculating a new maximum for the loaded element and determining if any remaining components further gate the maximum.
- 6. The method of Claim 4, wherein step of redetermining that gating occurs includes recalculating a new maximum for the reloaded element and determining if any remaining components further gate the maximum.
- 7. The method of Claim 4, wherein the step of merging the elements results in an elemental block that is a sub-plan of the overall plan, but which is a function of a single variable.

- 8. The method of Claim 7, wherein the merged elements intersect at a common resource in the transformed space.
- 9. The method of Claim 1, wherein the expected value function represents a statistical expectation of the value function at a given resource allocation and for a given demand distribution.
- 10. The method of Claim 1, wherein the transforming step involves taking a transformation of the product space to provide the working transformed space wherein the distribution induced on the resources is transformed into a distribution with zero mean and unit variance.
- 11. The method of Claim 10, wherein the transformation includes an inverse Cholesky transformation of the product space to provide the working transformed space.
- 12. A method for optimizing a multivariate expected value function which represents a statistical expectation of the value function at a given component allocation and for a given demand distribution, the method comprising:

forming a plan in the product space associated with the expected value function which represents the products, components, and connectivities therebetween;

transforming the product space plan to form a corresponding working space plan, with products corresponding to elements such that the distribution induced on the resources is transformed into a distribution with zero mean and unit variance;

converting the associated expected value function into a closed from expression;

performing a loading step which loads each element with components that gate the production of each element;

performing a reloading step which reloads components that were unloaded from an element in the loading step;

merging elements that are further gated by components that were unloaded, with the loading, reloading, and merging steps resulting in an equilibrium configuration; and

solving the equilibrium configuration to determine the optimization of the expected value function.

- 13. The method of Claim 12, wherein the demand distribution includes any multivariate demand distribution that is a member of the elliptical family of distributions.
- 14. The method of Claim 13, wherein the multivariate demand distribution includes a multivariate normal distribution.
- 15. The method of Claim 12, wherein the transforming step includes using an inverse Cholesky transform.
 - 16. The method of Claim 12, wherein the loading step includes:

sequentially analyzing each element in the plan;

determining if each associated component gates production of the element,

if gating occurs, then unloading the component from a prior element if so loaded, and

loading the component onto the present element.

17. The method of Claim 16, wherein the reloading step further includes:

sequentially analyzing each element in the plan;
reloading each unloaded component back onto the element;
redetermining if the element is gated by each reloaded component.

- 18. The method of Claim 12, wherein the equilibrium configuration includes configuring of the plan into elemental blocks which are a function of a single variable.
- 19. The method of Claim 18, wherein each elemental block is maximized over this single variable.
- 20. The method of Claim 19, wherein the optimum level of components to support the maximizations are derived from the maximized elemental values.
- 21. A method for optimizing the multivariate amount of refinements produced from a level of resources, the method comprising:

configuring the refinements and resources in a representative refinement space plan that accounts for connectivities therebetween;

deriving an expected value function for the refinement space plan;

converting the expected value function to a closed form expression;

transforming the refinement space plan into a working space plan, with the refinements represented by transformed elements;

sequentially loading each element with resources that gate the production of each element;

sequentially reloading components that were unloaded from elements in the loading step;

merging elements that are further gated by components that were unloaded, with the loading, reloading, and merging steps resulting in an equilibrium configuration; and

solving the equilibrium configuration to determine the optimization of the expected value function.